

REPORT DOCUMENTATION PAGE				Form Approved OMB No. 0704-0188	
<p>The public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing the burden, to the Department of Defense, Executive Services and Communications Directorate (0704-0188). Respondents should be aware that notwithstanding any other provision of law, no person shall be subject to any penalty for failing to comply with a collection of information if it does not display a currently valid OMB control number.</p> <p>PLEASE DO NOT RETURN YOUR FORM TO THE ABOVE ORGANIZATION.</p>					
1. REPORT DATE (DD-MM-YYYY) 13-08-2009		2. REPORT TYPE Conference Proceeding		3. DATES COVERED (From - To)	
4. TITLE AND SUBTITLE Spatial Evolution of the Frequency Distribution of Dissipation and Implications on Frequency Domain Modeling				5a. CONTRACT NUMBER	
				5b. GRANT NUMBER	
				5c. PROGRAM ELEMENT NUMBER 0601153N	
6. AUTHOR(S) James M. Kaihatu, Jayaram Veeramony, Kacey L. Edwards				5d. PROJECT NUMBER	
				5e. TASK NUMBER	
				5f. WORK UNIT NUMBER 73-9198-08-5	
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) Naval Research Laboratory Oceanography Division Stennis Space Center, MS 39529-5004				8. PERFORMING ORGANIZATION REPORT NUMBER NRL/PP/7320-08-9144	
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES) Office of Naval Research 800 N. Quincy St. Arlington, VA 22217-5660				10. SPONSOR/MONITOR'S ACRONYM(S) ONR	
				11. SPONSOR/MONITOR'S REPORT NUMBER(S)	
12. DISTRIBUTION/AVAILABILITY STATEMENT Approved for public release, distribution is unlimited.					
13. SUPPLEMENTARY NOTES					
14. ABSTRACT <p>The evolution of the frequency dependence of dissipation coefficient α_n of shoaling and breaking waves is investigated. Prior studies have established the observation of, and physical reasoning behind, $\alpha_n \sim f^2$, or that the dissipation should be weighted as the square of the wave frequency in the spectrum. A recent study, however, showed that this weighting evolves over the shoaling and breaking zone, with $\alpha_n \sim f^2$ acting as an inner surf zone asymptote. Parameterization of the evolution of the weighting as a function of depth brings forward several questions, the most important being whether the surf of individual breaking events is equivalent to the total dissipation as described by lumped parameterizations. Overall generality of the parameterizations will require more data to establish.</p>					
15. SUBJECT TERMS parameterization, wave spectra, wave propagation					
16. SECURITY CLASSIFICATION OF:			17. LIMITATION OF ABSTRACT UL	18. NUMBER OF PAGES 9	19a. NAME OF RESPONSIBLE PERSON Jayaram Veeramony
a. REPORT Unclassified	b. ABSTRACT Unclassified	c. THIS PAGE Unclassified			19b. TELEPHONE NUMBER (Include area code) 228-688-4835

20090821533

PUBLICATION OR PRESENTATION RELEASE REQUEST

Pubkey: 6004

NRLINST 5600.2

1. REFERENCES AND ENCLOSURES	2. TYPE OF PUBLICATION OR PRESENTATION	3. ADMINISTRATIVE INFORMATION
Ref: (a) NRL Instruction 5600.2 (b) NRL Instruction 5510.40D Encl: (1) Two copies of subject paper (or abstract)	<input type="checkbox"/> Abstract only, published <input type="checkbox"/> Book <input type="checkbox"/> Conference Proceedings (refereed) <input type="checkbox"/> Invited speaker <input type="checkbox"/> Journal article (refereed) <input type="checkbox"/> Oral Presentation, published <input type="checkbox"/> Other, explain <input type="checkbox"/> Abstract only, not published <input type="checkbox"/> Book chapter <input checked="" type="checkbox"/> Conference Proceedings (not refereed) <input type="checkbox"/> Multimedia report <input type="checkbox"/> Journal article (not refereed) <input type="checkbox"/> Oral Presentation, not published	STRN <u>NRLPP/7320-08-9044</u> Route Sheet No. <u>7320/</u> Job Order No. <u>73-9198-08-5</u> Classification <input checked="" type="checkbox"/> X <input type="checkbox"/> U <input type="checkbox"/> C Sponsor <u>ONR</u> approval obtained: <input type="checkbox"/> yes <input checked="" type="checkbox"/> X <input type="checkbox"/> no

4. AUTHOR

Title of Paper or Presentation

Spatial Evolution of the Frequency Distribution of Dissipation and Implications on Frequency Domain Modeling

Author(s) Name(s) (First, MI, Last), Code, Affiliation if not NRL

James M. Kaihatu, Jayaram Veeramony, Kacey L. Edwards

It is intended to offer this paper to the Proceedings of ICCE 2008 Conference

(Name of Conference)

(Date, Place and Classification of Conference)

and/or for publication in Proceedings of ICCE 2008 Conference, Unclassified

(Name and Classification of Publication)

(Name of Publisher)

After presentation or publication, pertinent publication/presentation data will be entered in the publications data base, in accordance with reference (a).

It is the opinion of the author that the subject paper (is ☐) (is not ☒ X) classified, in accordance with reference (b).This paper does not violate any disclosure of trade secrets or suggestions of outside individuals or concerns which have been communicated to the Laboratory in confidence. This paper (does ☐) (does not ☒ X) contain any militarily critical technology. This subject paper (has ☐) (has never ☒ X) been incorporated in an official NRL Report.

Jayaram Veeramony, 7322

Name and Code (Principal Author)

(Signature)

5. ROUTING/APPROVAL			
CODE	SIGNATURE	DATE	COMMENTS
Author(s) <u>Veeramony</u>	<u>[Signature]</u>	<u>12/3/2008</u>	Need by <u>23 Dec 08</u> Publicly accessible sources used for this publication <u>Proceedings of previous conference</u>
Section Head <u>Allard</u>	<u>[Signature]</u>	<u>12-5-08</u>	
Branch Head Gregg A. Jacobs, 7320 <u>(Barr)</u>	<u>[Signature]</u>	<u>12-8-08</u>	
Division Head Ruth H. Preller, 7300	<u>[Signature]</u>	<u>12-8-08</u>	1. Release of this paper is approved. 2. To the best knowledge of this Division, the subject matter of this paper (has <input type="checkbox"/>) (has never <input checked="" type="checkbox"/> X) been classified.
Security, Code 1226	<u>[Signature]</u>	<u>12/11/08</u>	1. Paper or abstract was released. 2. A copy is filed in this office. <u>SSC 455-8</u>
Office of Counsel, Code 1008.3			
ADOR/Director NCST E. R. Franchi, 7000			
Public Affairs (Unclassified/ Unlimited Only). Code 7030.4			
Division, Code			
Author, Code			

PUBLICATION OR PRESENTATION RELEASE REQUEST

08-1226-3988

Key: 6004

NRLINST 5600.2

Ref: (a) NRL Instruction 5600.2 (b) NRL Instruction 5519.40D	() Abstract only, published () Book () Conference Proceedings (refereed) () Invited speaker () Journal article (refereed) () Oral Presentation, published () Other, explain	() Abstract only, not published () Book chapter (X) Conference Proceedings (not refereed) () Multimedia report () Journal article (not refereed) () Oral Presentation, not published	STRN <u>NRLPP7320-08-9044</u> Route Sheet No. <u>7320/</u> Job Order No. <u>73-9198-08-5</u> Classification <u>X</u> <u>U</u> Sponsor <u>ONR Basic 6.1</u> approval obtained <u>yes</u> <u>X</u> <u>no</u>
-----------------------------------------------------------------	------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------	----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------	---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------

Title of Paper or Presentation

Spatial Evolution of the Frequency Distribution of Dissipation and Implications on Frequency Domain Modeling

Author(s) Name(s) (First, Mi. Last), Code, Affiliation if not NRL

James M. Kallatu, Jayaram Veeramony, Kacey L. Edwards

This is a Final Security Review.
Any changes made in the document
after approved by Code 1226
the Security Review.

It is intended to offer this paper to the Proceedings of ICCE 2008 Conference

(Name of Conference)

(Date, Place and Classification of Conference)

and/or for publication in Proceedings of ICCE 2008 Conference, Unclassified

(Name and Classification of Publication)

(Name of Publisher)

After presentation or publication, pertinent publication/presentation data will be entered in the publications data base, in accordance with reference (a).

It is the opinion of the author that the subject paper (is) (is not X) classified, in accordance with reference (b).

This paper does not violate any disclosure of trade secrets or suggestions of outside individuals or concerns which have been communicated to the Laboratory in confidence. This paper (does) (does not X) contain any military critical technology.
This subject paper (has) (has never X) been incorporated in an official NRL Report.

Jayaram Veeramony, 7322

Name and Code (Principal Author)

(Signature)

CODE	SIGNATURE	DATE	COMMENTS
Author(s) <u>Veeramony</u>	<u>Jayaram</u>	<u>12/3/2008</u>	Need by <u>22 Dec 08</u> Publicly accessible sources used for this publication <u>Proceedings of previous conference</u>
Section Head <u>Allard</u>	<u>Paul Allard</u>	<u>12-5-08</u>	
Branch Head Gregg A. Jacobs, 7320 (<u>Barton</u>)	<u>Charlie Barton</u>	<u>12-8-08</u>	
Division Head Ruth H. Preller, 7300	<u>Bill B. Preller</u>	<u>12-8-08</u>	1. Release of this paper is approved. 2. To the best knowledge of this Division, the subject matter of this paper (has <u> </u>) (has never <u>X</u>) been classified.
Security, Code 1226	<u>Shawn Rogers</u>	<u>12/11/08</u>	1. Paper or abstract was released. 2. A copy is filed in this office. <u>SSC 455-8</u>
Office of Counsel, Code 1088.3	<u>W. Beede</u>	<u>12/11/08</u>	
ADGR/Director, NSST E. R. Franchi, 7000	<u>Rob Franchi</u>	<u>12/12/08</u>	
Public Affairs (Unclassified/ Unlimited Only), Code 7030.4			
Division, Code			
Author, Code			

S

vol. 1

Proceedings of the 31st International Conference

Coastal Engineering 2008

Hamburg, Germany 31 August – 5 September 2008



edited by
Jane McKee Smith
U.S. Army Engineer Research and Development Center
Coastal & Hydraulics Laboratory
USA

 **World Scientific**

NEW YORK LONDON SINGAPORE

ACKNOWLEDGMENTS

The Office of Naval Research and the National Council of Science and Technology of Mexico provided financial support for this study. Marien Boers is gratefully acknowledged for providing his laboratory data. J.L. Lara is indebted to the M.E.C. for the funding provided in the Ramon y Cajal Program. I. J. Losada would like to thank to the Spanish Ministry of Ciencia e Innovación for the funding associated to the project "Experimental and numerical modelling of surf zone hydrodynamics", CTM2008-06044/MAR.

REFERENCES

- Battjes, J., H.J. Bakkenes, T. T. Janssen, and A. R. van Dongeren. 2004. Shoaling of subharmonic gravity waves. *J. Geophys. Res.*, 109.
- Boers, M. 1996. Simulation of a surf zone with a barred beach, part 1: Wave heights and wave breaking. *Rep. 96-5*, 116 pp., Comm. on Hydrol. And Geol. Eng., Dep. of Civ. Eng., Delft Univ. of Technol., Delft, Netherlands.
- Elgar, S. and B. Raubenheimer. 2008. Wave dissipation by muddy seafloors. *Geophys. Res. Lett.* 35, L07611.
- Janssen, T.T., J.A. Battjes, and A. R. van Dongeren. 2003. Long waves induced by short-wave groups over a sloping bottom. *J. Geophys. Res.* 108.
- Lin, P. and P. L.-F. Liu. 1998. A numerical study of breaking waves in the surf zone. *J. Fluid Mech.* 359, 239-264.
- Longuet-Higgins, M. S. and R. W. Stewart. 1962. Radiation stress and mass transport in gravity waves with application to surf beats. *J. Fluid Mech.*, 8, 565-583.
- Losada, I. J., J. L. Lara, R. Guanche and J. M. González-Ondina. 2008. Numerical analysis of wave overtopping of high mound breakwaters. *Coastal Eng.* 55, 47-62.
- Madsen, P. A., O. R. Sørensen and H. A. Schaffer. 1997. Surf zone dynamics simulated by a Boussinesq type model: part 2. Surf beat and swash oscillations for wave groups and irregular waves. *Coast. Eng.*, 32, 289-319.
- Munk, W. H. 1949. Surf beats. *Trans Am. Geophys. Union*, 30, 849-854.
- Schaffer, H. A. 1993. Infragravity waves induced by short wave groups. *J. Fluid Mech.*, 247, 551-588.
- Symonds, G., D. A. Huntley and A. J. Bowen. 1982. Two-dimensional surf beat: long wave generation by a time-varying breakpoint. *J. Geophys. Res.* 87, 492-498.
- Torres-Freyermuth, A., I. J. Losada, and J. L. Lara. 2007. Modelling of surf zone processes on a natural beach using RANS equations. *J. Geophys. Res.* 112.
- Hsu, T.-J., P. A. Traykovsky, and G. C. Kineke. 2007. On modelling boundary layer and gravity-driven fluid mud transport. *J. Geophys. Res.* 112.
- Watson, G. and D. H. Peregrine. 1992. Low-freq waves in the surf zone. *Proc. 23rd Int. Conf. Coastal Engineering*, pp. 818-831. ASCE.

SPATIAL EVOLUTION OF THE FREQUENCY DISTRIBUTION OF DISSIPATION AND IMPLICATIONS ON FREQUENCY DOMAIN MODELING

James M. Kaihatu¹, Jayaram Veeramony² and Kacey L. Edwards²

The evolution of the frequency dependence of dissipation coefficient α_s of shoaling and breaking waves is investigated. Prior studies have established the observation of, and physical reasoning behind, $\alpha_s \sim f^2$, or that the dissipation should be weighted as the square of the wave frequency in the spectrum. A recent study, however, showed that this weighting evolves over the shoaling and breaking zone, with $\alpha_s \sim f^2$ acting as an inner surf zone asymptote. Parameterization of the evolution of the weighting as a function of depth brings forward several questions, the most important being whether the sum of individual breaking events is equivalent to the total dissipation as described by lumped parameterizations. Overall generality of the parameterizations will require more data to establish.

INTRODUCTION

Wave Breaking and Wave Spectra

Waves in the nearshore are significantly modified by nonlinear interactions, transitioning from quasi-sinusoidal forms to cnoidal-type forms, with markedly flatter troughs and peaked crests. These processes are caused by nonlinear wave-wave interactions among triads of frequencies. These interactions occur at length scales of $O(m)$, in contrast to the $O(km)$ length scales of quartet interactions of deep water waves. As these waves approach the shoreline, they reach a limiting height and break; the type of breaking ranges from gentle spilling breakers to violent plunging breaking. The breaking leads to a release of momentum into the water column, and is responsible for the generation of nearshore currents, the transport of sediments, and bathymetric change.

The transformations described above are reflected in wave spectra measurements (Freilich and Guza 1984). These processes are manifested in the changes of the spectral shape. Harmonics of the spectral peak are amplified due to superharmonic nonlinear interaction during shoaling. Low frequencies are also amplified as long wave motions are generated by nonlinear interactions. In the surf zone, the high frequency energy begins to decrease as dissipation continues. Smith and Vincent (2003), using wavenumber spectra derived from recorded frequency spectra in the laboratory and field, determined that the shape of the spectra in the surf zone had characteristic shapes explicable by the theories of

¹ Zachry Department of Civil Engineering, Texas A&M University, 3136 TAMU, College Station, TX, 77843-3136, USA

² Oceanography Division (Code 7322), Naval Research Laboratory, Stennis Space Center, MS, 38628-5004, USA

Toba (1973) and Zakharov (1999). In contrast, Kaihatu et al. (2007), using the data of Bowen and Kirby (1994) and Mase and Kirby (1992), showed how the wave spectra reached an asymptotic shape in the inner surf zone, where the high frequency tail appeared to have a slope proportional to f^{-2} , in accord with the observation of a sawtooth wave (Kirby and Kaihatu 1996). Interestingly, however, this value was not constant throughout the surf zone, but varied through the surf zone as the depth changed.

Kirby and Kaihatu (1996) developed a method of evaluating the frequency-dependent dissipation from data, assuming that the dissipation was primarily that due to eddy viscosity, in the manner of Zelt (1991). The resulting mechanism demonstrated an inverse relationship between the frequency dependence of dissipation and the shape of the frequency spectrum. Along with the correspondence between sawtooth waves and the associated f^{-2} dependence on the spectral variance, Kirby and Kaihatu (1996) demonstrated that the optimal frequency distribution for the dissipation is f^{-2} . Chen et al. (1997) tested this assumed distribution with data by using various distributions in a nonlinear wave transformation model (Chen and Liu 1995) and comparing them to data. They determined that the f^{-2} worked best.

Interestingly, though, Kaihatu et al. (2007) showed that, while the inverse relationship between spectral slope and dissipation frequency dependence was evident, the frequency dependence of the dissipation evolved through the surf zone. The f^{-2} -weighted dependence for dissipation was the asymptote in the very nearshore.

Frequency Domain Models and Dissipation

Numerical models of nonlinear wave propagation are generally divided into time-domain and frequency domain formulations. Time domain models evolve the free surface as a function of time and space; extended Boussinesq models such as Madsen et al. (1991), Nwogu (1993), Wei et al. (1995) and Lynett and Liu (2004) fall into this category. These models have the advantage of allowing non-periodic waves and currents to be simulated, but can also be numerically complex. Frequency-domain models, in contrast, assume time-periodic motion from the outset. Triad resonance is assumed in order to completely factor out time dependence from the model, allowing explicit formulation of the three-wave interaction terms.

Frequency domain models require a spectral dissipation mechanism (e.g., Battjes and Janssen 1978; Thornton and Guza 1983). Generally these mechanisms are only functions of integrated parameters of the spectrum. No frequency dependence is specified, so it is generally assumed that the dissipation is either applied as a constant over frequency, or is weighted as frequency squared. This latter weighting was found by Chen et al. (1997) to provide accurate results for not only frequency spectra, but also with wave shape statistics such as skewness and asymmetry. However, since Kaihatu et al. (2007)

showed evolution of the dissipation's frequency dependence through the surf zone, it would be interesting to see how this evolution affects the models.

In this study we investigate the trends in the slope of the spectral tail for shoaling and breaking waves, with an emphasis on the implications for numerical modeling of nonlinear shoaling and breaking waves

LABORATORY EXPERIMENTS

Bowen and Kirby (1994)

Bowen and Kirby (1994) conducted several laboratory experiments, in which single peaked wave spectra were generated in a laboratory flume and allowed to propagate over a sloping bottom. The layout of the experiment is shown in Figure 1. Three different incident wave conditions (referred to as Case A, B and C) were generated at the wave maker; the measurement procedures for each case were identical. One feature of this experiment is the dense coverage of data in the surf zone. Free surface elevations were measured at 47 locations in the tank by utilizing a carriage situated on two rails on the top edge of the tank, and moving it in increments.

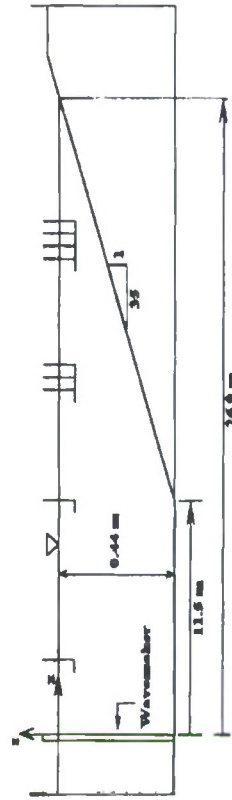


Figure 1. Experimental layout of Bowen and Kirby (1994).

Data were taken at 25 Hz for approximately 17 minutes, with the first 925 points disregarded to allow the domain to fill up with waves. The resulting records were each divided into 12 realizations of 2,048 points apiece. Frequency spectra were calculated for each realization, averaged over the realizations, and then averaged over eight adjacent bands, leading to 192 degrees of freedom. Spectra from the data are shown in Figure 2 (Case B).

ANALYSIS

Frequency Dependent Dissipation Coefficient from Data

Many frequency domain shoaling wave models (e.g. Agnon et al. 1993; Kaihatu and Kirby 1995) have the following form:

$$\frac{\partial A_n}{\partial x} + \frac{1}{2C_g} \frac{\partial C_g}{\partial x} A_n + \alpha_n A_n = nJ \text{ terms} \quad (1)$$

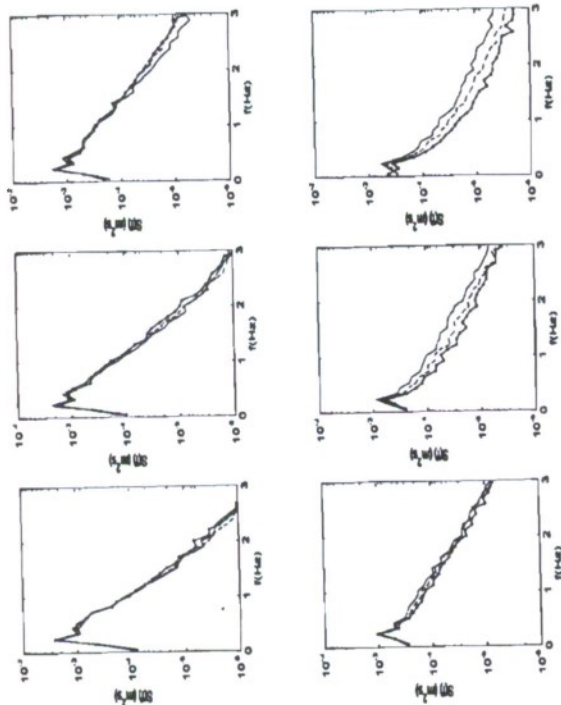


Figure 2. Various frequency spectra from the experiment of Bowen and Kirby (Case B). Water depth reduces successively from upper left to lower right. Different line types denote different adjacent gauges.

Kirby and Kaihatu (1996), assuming that the nature of the dissipation can be adequately described by an eddy viscosity mechanism (Zelt 1991) determined that the instantaneous dissipation ε_b can be calculated from the free surface elevation as:

$$\varepsilon_b = -\rho \left(\frac{\eta}{h} \right) \frac{\partial}{\partial t} \left(v_b \frac{\partial \eta}{\partial t} \right) \quad (2)$$

in which v_b is an eddy viscosity developed as a function of the slope of the free surface elevation in time. Kirby and Kaihatu (1996) further develop this into an expression that relates the dissipation coefficient α_n to the dissipation spectrum $S(f)$ and the free surface spectrum $S(\eta)$:

$$\alpha_n = \frac{1}{\rho g \sqrt{gh}} \frac{1}{\sqrt{\Delta f}} \frac{\sqrt{S_e(n\Delta f)}}{S(n\Delta f)} \quad (3)$$

where n is the integer multiple of the frequency resolution Δf . Note in Equation (3) that the dissipation coefficient α_n and the spectral density $S(n\Delta f) = S(f)$ are inversely related. Kaihatu et al. (2007) showed that the inverse nature of these relationships was strongest in the inner surf zone, where $\alpha_n \sim f^{-2}$ and $S(f) \sim f^2$.

Evolution of Frequency Dependence of Dissipation with Depth

One immediate method for incorporating this evolution of the frequency dependence into modeling is to fit curves through the measured evolution of the frequency dependence of the dissipation coefficient in the model. In the model of Kaihatu and Kirby (1995), this is achieved via the following:

$$\alpha_n = \frac{f_n^m}{f_p^m} \beta(x) \left[\frac{f_p^m \sum_{n=1}^N |A_n|^2}{\sum_{n=1}^N f_n^m |A_n|^2} \right] \quad (4)$$

in which m is the exponent of frequency dependence. For the case of frequency-dependent dissipation coefficient studied by Kirby and Kaihatu (1996) and Chen et al. (1997), $m = 2$. The term $\beta(x)$ is the total dissipation in the wavefield due to breaking at any location x ; this can be described by such lumped parameter descriptions as Battjes and Janssen (1978) and Thornton and Guza (1983), but requires modification to fit within the context of frequency domain models (Mase and Kirby 1992; Kaihatu and Kirby 1995; Eldeberky and Battjes 1996).

As done in Kaihatu et al. (2007), the frequency dependence of α_n was found by performing a power fit for the frequency range from zero up to one-half of the Nyquist frequency. The resulting power fits were then themselves curve-fit as a function of water depth. Two curve fits of these frequency dependencies were performed for each of the three cases of the Bowen and Kirby (1994) experiments. The result for Case B is shown in Figure 3. It is apparent that the frequency dependence of dissipation undergoes substantial evolution over the shoaling and breaking region. However, use of this information in frequency domain models via (4) assumes that equivalence exists between the integral of instantaneous dissipation events (Equation 2) and the total lumped parameter dissipation mechanism of Battjes and Janssen (1978) or Thornton and Guza (1983). This is not entirely clear. Most models using lumped energy parameterizations for breaking assume that averaging of the individual breaking events leads to the parameterization. This is, in general, not guaranteed. This is particularly true when nonlinearity is taken into account; any preferential frequency distribution of the dissipation will affect inter-frequency wave-wave

interaction. Kirby and Kaihatu (1996) note that individual breaking events can impart a discrete "kick" into the water column; if these discrete events are widely spaced in time, they can themselves generate low frequency motions. These events would likely not be represented in an integrated bulk parameterization.

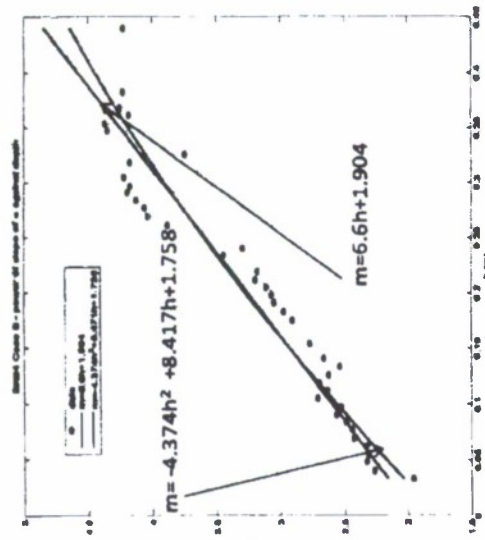


Figure 3. Curve fits of m to depth (on x axis) for Case B of Bowen and Kirby (1994). Solid lines are two potential curve fits of m to depth. Asterisks are values of m taken from individual frequency spectra at gage locations. Frequency range for calculations of m at each location is from $f=0$ to one-half the Nyquist frequency.

In practical modeling of these issues, it is not likely that frequencies up to one-half the Nyquist frequency would be included, as this would generally require $O(500)$ frequency components to be retained. Bredmose (2002) noted that the number of computations required for nonlinear frequency domain models were on the order of $O(N^2)$, where N is the total number of frequency components. Typically, around 200 frequencies would be retained for the nonlinear frequency domain models, which, in the case of Bowen and Kirby (1994) would result in a maximum frequency of 2.4 Hz, about three times the peak frequency. However, this would also imply that the frequency range over which the dissipation α_n would be calculated would also be concomitantly smaller. To investigate this, the frequency range for the calculation of the exponent m was limited to between 0 and 2.4 Hz. The values of m were then recalculated, and then plotted as a function of the water depth. This plot, along with the trial curve fits, is shown in Figure 4. It is clear that this is quite different than the previous result in Figure 4. The impact on modeling is thus not clear, especially since the accurate modeling of high frequency evolution is important for reliable wave shape statistics (Kaihatu and Kirby 1996). It is likely that the

large coefficients of the fourth-order polynomial will cause some difficulty with the numerical solution. In any event, more data will be needed to provide a clearer picture of whether or not a parameterization in this manner is sensible.

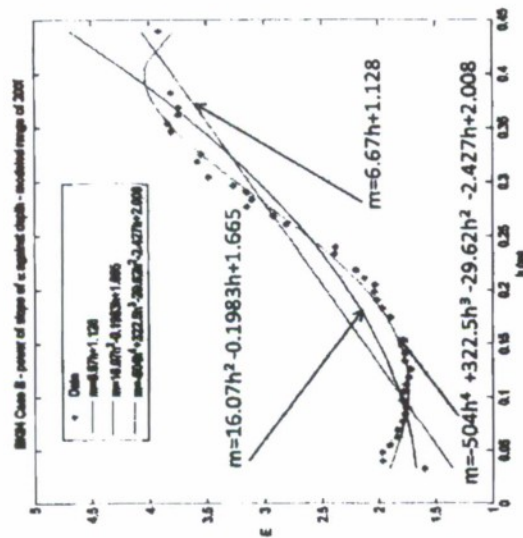


Figure 4. Curve fits of m as a function of water depth, Bowen and Kirby (1994) Case B. Solid lines are trial curve fits for m as a function of h . Asterisks are values of m calculated from spectra between $f=0$ and $f=2.4$ Hz, or 200 frequencies.

CONCLUSIONS AND FUTURE WORK

The issue of the frequency dependence of dissipation coefficient α_n was addressed in this study, particularly as regards its impact on frequency domain numerical wave modeling. Kirby and Kaihatu (1996) discussed the choice of α_n , in concert with the inverse relationship between the spectral shape and the frequency dependence of α_n . This was confirmed with numerical simulations by Chen et al. (1997) and with additional data analysis by Kaihatu et al. (2007). The latter study also demonstrated the evolution of this frequency dependence of α_n , implying that improvement can be made by replicating this evolution in the frequency domain models via Equation (4). Analysis of the data in this regard reveals that a) an equivalence between the integral over individual instantaneous breaking events, and a lumped parameterization describing overall dissipation, needs to be established; and b) the number of retained frequency components in modeling has a significant effect on the form of the parameterized frequency distribution. The adequacy of these descriptions remains to be seen, and will require more data to establish.

It can also be argued that a well-suited alternative to this approach would be to allow the time-dependent breaking mechanism to establish its own statistics.

For frequency domain models, this would entail using a hybrid time/frequency domain modeling approach, similar to that of Bredmose (2003). This would allow breaking parameters to be calculated based on local front face slopes (Zelt 1991) and not on presumed frequency distributions of lumped dissipation parameters. This approach is presently being pursued.

ACKNOWLEDGMENTS

JMK was supported by Texas Engineering Experiment Station. JV and KLE were supported by 6.1 NRL Core Project "Spilling Breakers," Program Element #T046-07.

REFERENCES

- Agnon, Y., A. Sheremet, J. Gonsalves, and M. Stiassnie. 1993. Nonlinear evolution of a unidirectional shoaling wave field. *Coastal Engineering*, 20, 29-58.
- Battjes, J.A., and J.P.F.M. Janssen. 1978. Energy loss and set-up due to breaking of random waves. *Proceedings of 14th International Conference on Coastal Engineering*, ASCE, 466-480.
- Bowen, G.D. and J.T. Kirby. 1994. Shoaling and breaking random waves on a 1:35 laboratory beach. *Tech. Rep. No. CACR-94-14*, Center for Applied Coastal Research, Department of Civil Engineering, University of Delaware.
- Bredmose, H. 2003. *Deterministic modeling of water waves in the frequency domain*. PhD Thesis, Technical University of Denmark, Denmark.
- Chen, Y. and P. L.-F. Liu. 1995. Modified Boussinesq equations and associated parabolic models for water wave propagation. *Journal of Fluid Mechanics*, 288, 351-381.
- Chen, Y., R.T. Guza and S. Elgar. 1997. Modeling spectra of breaking surface waves in shallow water. *Journal of Geophysical Research*, 102, 25035-25046.
- Eldeberky, Y., and J.A. Battjes. 1996. Spectral modeling of wave breaking: application to Boussinesq equations. *Journal of Geophysical Research*, 101, 1253-1264.
- Freilich, M.H. and R.T. Guza. 1984. Nonlinear effects on shoaling surface gravity waves. *Philosophical Transactions of the Royal Society of London*, A311, 1-41.
- Kaihatu, J. M. and J.T. Kirby. 1995. Nonlinear transformation of waves in finite water depth. *Physics of Fluids*, 7, 1903-1914.
- Kaihatu, J. M., J. Veeramony, K. L. Edwards, and J. T. Kirby. 2007. Asymptotic behavior of frequency and wave number spectra of nearshore shoaling and breaking waves. *Journal of Geophysical Research*, 112, C06016. doi:10.1029/2006JC003817.

- Kirby, J.T. and J. M. Kaihatu. 1996. Structure of frequency domain models for random wave breaking. In B.L. Edge (Ed.), *Proceedings of the 25th International Conference of Coastal Engineering*, (pp. 1144-1155). Reston, VA: American Society of Civil Engineers.
- Lynett, P.J., and P. L.-F. Liu. 2004. A two-layer approach to water wave modeling. *Proceedings of the Royal Society of London, Series A*, 460, 2637-2669.
- Madsen, P.A., R. Murray, and O.R. Sørensen. 1991. A new form of Boussinesq equations with improved dispersion characteristics. *Coastal Engineering*, 15, 371-388.
- Mase, H. and J.T. Kirby. 1992. Hybrid frequency-domain KdV equation for random wave transformation. In B. L. Edge (Ed.), *Proceedings of the 23rd International Conference of Coastal Engineering* (pp. 474-487). Reston, VA: American Society of Civil Engineers.
- Nwogu, O. 1993. An alternative form of the Boussinesq equations for nearshore wave propagation. *ASCE Journal of Waterway, Port, Coastal and Ocean Engineering*, 119, 618-638.
- Smith, J.M. and C.L. Vincent. 2003. Equilibrium ranges in surf zone wave spectra. *Journal of Geophysical Research*, 108, 3366-3376.
- Thornton, E.B. and R.T. Guza. 1983. Transformation of wave height distribution. *Journal of Geophysical Research*, 88, 5925-5938.
- Toba, Y. 1973. Local balance in the air-sea boundary processes on the spectrum of wind waves. *Journal of Oceanographic Society of Japan*, 29, 209-220.
- Wei, G., J.T. Kirby, S.T. Grilli, and R. Subramanya. 1995. A fully nonlinear Boussinesq model for surface waves. I. Highly nonlinear, unsteady waves. *Journal of Fluid Mechanics*, 294, 71-92.
- Zakharov, V. 1999. Statistical theory of gravity and capillary waves on the surface of a finite depth fluid. *European Journal of Mechanics, B: Fluids*, 18, 327-344.
- Zelt, J.A. 1991. The run-up of nonbreaking and breaking solitary waves. *Coastal Engineering*, 15, 205-246.